Laboratory Exercise 6

Adders, Subtractors, and Multipliers

The purpose of this exercise is to examine arithmetic circuits that add, subtract, and multiply numbers. Each circuit will be described in VHDL and implemented on an Intel[®] FPGA DE10-Lite, DE0-CV, DE1-SoC, or DE2-115 board.

Part I

Consider again the four-bit ripple-carry adder circuit used in lab exercise 2; its diagram is reproduced in Figure 1.



Figure 1: A four-bit ripple carry adder.

This circuit can be implemented using a '+' sign in VHDL. For example, the following code fragment adds *n*-bit numbers A and B to produce outputs sum and carry:

```
LIBRARY ieee;
USE ieee.std_logic_1164.all;
USE ieee.std_logic_arith.all;
USE ieee.std_logic_signed.all;
...
SIGNAL sum : STD_LOGIC_VECTOR(n-1 DOWNTO 0);
...
sum <= A + B;
```

Use this construct to implement a circuit shown in Figure 2. This circuit, which is often called an *accumulator*, is used to add the value of an input A to itself repeatedly. The circuit includes a carry out from the adder, as well as an *overflow* output signal. If the input A is considered as a 2's-complement number, then *overflow* should be set to 1 in the case where the output *sum* produced does not represent a correct 2's-complement result.

Perform the following steps:

- 1. Create a new Quartus[®] project. Write VHDL code that describes the circuit in Figure 2.
- 2. Connect input A to switches SW_{7-0} , use KEY_0 as an active-low asynchronous reset, and use KEY_1 as a manual clock input. The sum from the adder should be displayed on the red lights $LEDR_{7-0}$, the registered carry signal should be displayed on $LEDR_8$, and the registered *overflow* signal should be displayed on $LEDR_9$. Show the registered values of A and S as hexadecimal numbers on the 7-segment displays HEX3-2 and HEX1 0.

- 3. Make the necessary pin assignments needed to implement the circuit on your DE-series board, and compile the circuit.
- 4. Use timing simulation to verify the correct operation of the circuit. Once the simulation works properly, download the circuit onto your DE-series board and test it by using different values of *A*. Be sure to check that the *overflow* output works correctly.



Figure 2: An eight-bit accumulator circuit.

Part II

Extend the circuit from Part I to be able to both add and subtract numbers. To do so, introduce an *add_sub* input to your circuit. When *add_sub* is 1, your circuit should subtract A from S, and when *add_sub* is 0 your circuit should add A to S as in Part I.

Part III

Figure 3a gives an example of paper-and-pencil multiplication $P = A \times B$, where A = 11 and B = 12.

					x	$a_3 \\ b_3$	$egin{array}{c} a_2 \ b_2 \end{array}$	$\begin{array}{c} a_1 \\ b_1 \end{array}$	$a_0 \\ b_0$
$\begin{array}{c} x & \frac{1}{1} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \\ 1 & 1 \\ \hline 1 & 3 & 2 \end{array}$	$\begin{array}{c} \mathbf{x} \begin{array}{c} 1 0 1 1 \\ 1 1 0 0 \\ \hline 0 0 0 0 \\ 0 0 0 0 \\ 1 0 1 1 \\ 1 0 1 1 \\ \end{array}$		<i>a</i> ₃ <i>b</i> ₃	$a_3b_2 \\ a_2b_3$	$a_3b_1a_2b_2a_1b_3$	$\begin{array}{c} a_3b_0\\a_2b_1\\a_1b_2\\a_0b_3\end{array}$	$a_2b_0a_1b_1a_0b_2$	$a_1b_0\\a_0b_1$	<i>a</i> ₀ <i>b</i> ₀
		<i>p</i> ₇	p_6	<i>p</i> ₅	p_4	<i>p</i> ₃	p_2	p_1	p_0
a) Decimal	b) Binary	c) Implementation							



We compute $P = A \times B$ as an addition of summands. The first summand is equal to A times the ones digit of B. The second summand is A times the tens digit of B, shifted one position to the left. We add the two summands to form the product P = 132.

Part b of the figure shows the same example using four-bit binary numbers. To compute $P = A \times B$, we first form summands by multiplying A by each digit of B. Since each digit of B is either 1 or 0, the summands are either shifted versions of A or 0000. Figure 3c shows how each summand can be formed by using the Boolean AND operation of A with the appropriate bit of B.

A four-bit circuit that implements $P = A \times B$ is illustrated in Figure 4. Because of its regular structure, this type of multiplier circuit is called an *array multiplier*. The shaded areas correspond to the shaded columns in Figure 3*c*. In each row of the multiplier AND gates are used to produce the summands, and full adder modules are used to generate the required sums.



Figure 4: An array multiplier circuit.

Perform the following steps to implement the array multiplier circuit:

- 1. Create a new Quartus project.
- 2. Generate the required VHDL file. Use switches SW_{7-4} to represent the number A and switches SW_{3-0} to represent B. The hexadecimal values of A and B are to be displayed on the 7-segment displayes *HEX2* and

*HEX*0, respectively. The result $P = A \times B$ is to be displayed on *HEX*5 - 4.

- 3. Make the necessary pin assignments needed to implement the circuit on your DE-series board, and compile the circuit.
- 4. Use simulation to verify your design.
- 5. Download your circuit onto your DE-series board and test its functionality.

Part IV

In Part III, an array multiplier was implemented using full adder modules. At a higher level, a row of full adders functions as an n-bit adder and the array multiplier circuit can be represented as shown in Figure 5.



Figure 5: An array multiplier implemented using *n*-bit adders.

Each *n*-bit adder adds a shifted version of A for a given row and the *partial product* of the row above. Abstracting the multiplier circuit as a sequence of additions allows us to build larger multipliers. The multiplier should consist

of n-bit adders arranged in a structure shown in Figure 5. Use this approach to implement an 8×8 multiplier circuit with registered inputs and outputs, as shown in Figure 6.



Figure 6: A registered multiplier circuit.

Perform the following steps:

- 1. Create a new Quartus project and write the required VHDL file.
- 2. Use switches SW_{7-0} to provide the data inputs to the circuit. Use SW_9 as the enable signal *EA* for register *A*, and use SW_8 as the enable for register *B*. When $SW_9 = 1$ display the contents of register A on the red lights LEDR, and display the contents of register B on these lights when $SW_8 = 1$. Use KEY_0 as a synchronous reset input, and use KEY_1 as a manual clock signal. Show the product $P = A \times B$ as a hexadecimal number on the 7-segment displays *HEX3-0*.
- 3. Make the necessary pin assignments needed to implement the circuit on your DE-series board, and compile the circuit.
- 4. Test the functionality of your design by inputting various data values and observing the generated products.

Part V

Part IV showed how to implement multiplication $A \times B$ as a sequence of additions, by accumulating the shifted versions of A one row at a time. Another way to implement this circuit is to perform addition using an adder tree. An adder tree is a method of adding several numbers together in a parallel fashion. This idea is illustrated in Figure 7. In the figure, numbers A, B, C, D, E, F, G, and H are added together in parallel. The addition A + B happens simultaneously with C + D, E + F and G + H. The result of these operations are then added in parallel again, until the final sum P is computed.



Figure 7: An example of adding 8 numbers using an adder tree.

In this part you are to implement an 8×8 multiplier circuit by using the adder-tree approach. Inputs A and B, as well as the output P should be registered as in Part IV.

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